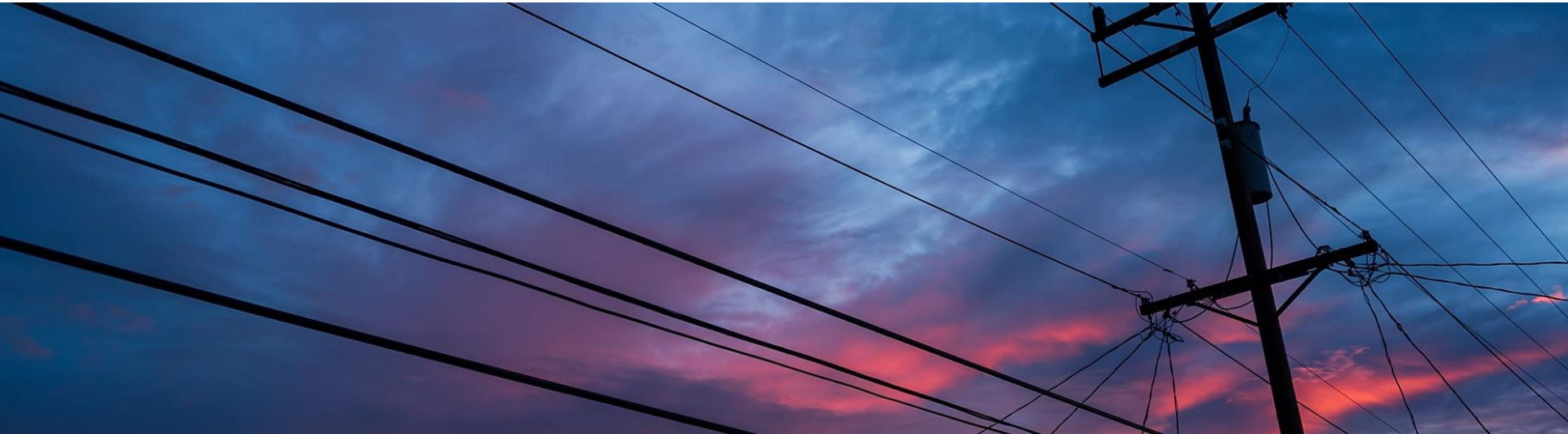


# *State Estimation in the Power Distribution System*

Towards a Data-Driven Application in the Low Voltage Grid



**Dominik Danner**

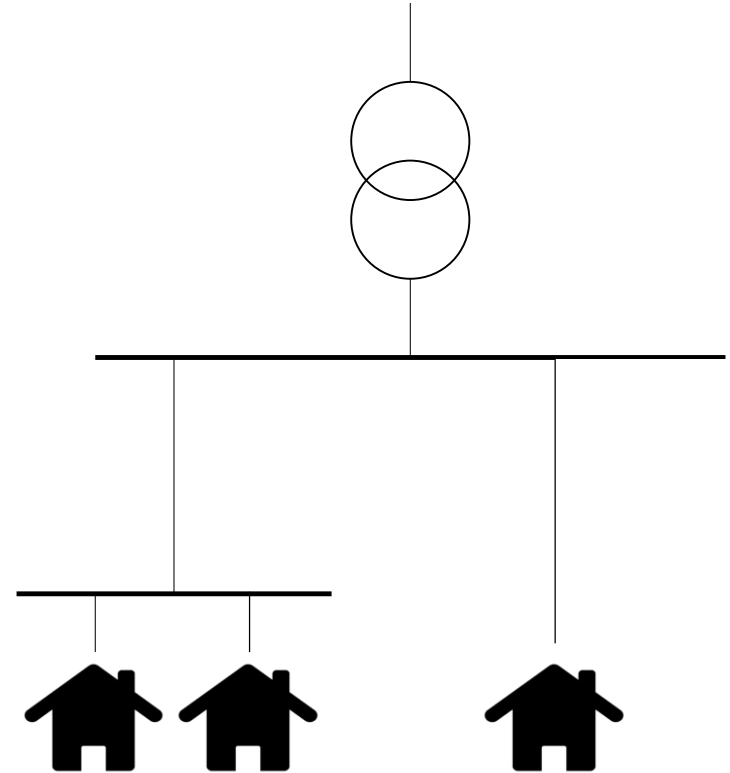
University of Passau

**Hermann de Meer**

University of Passau

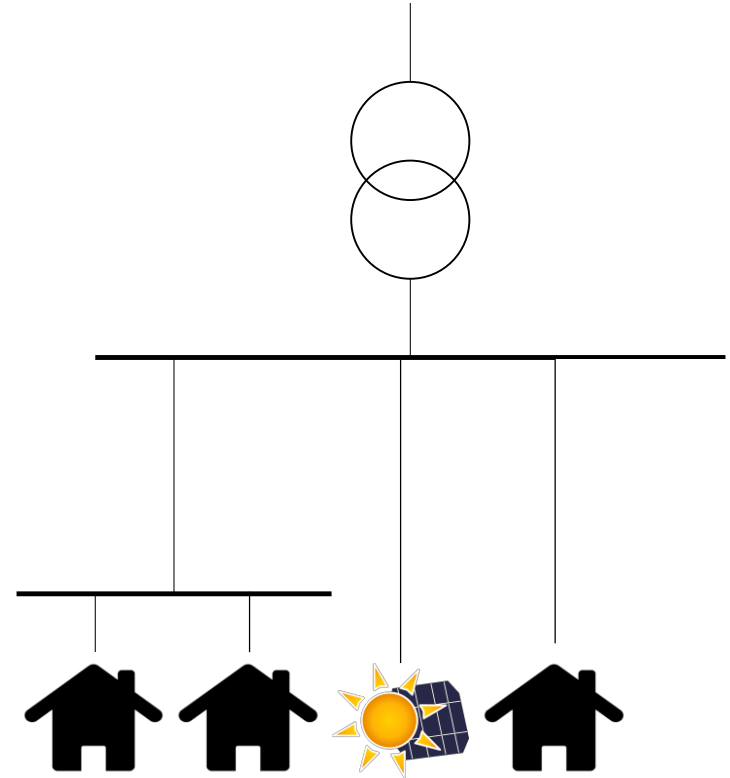


# 1. Motivation



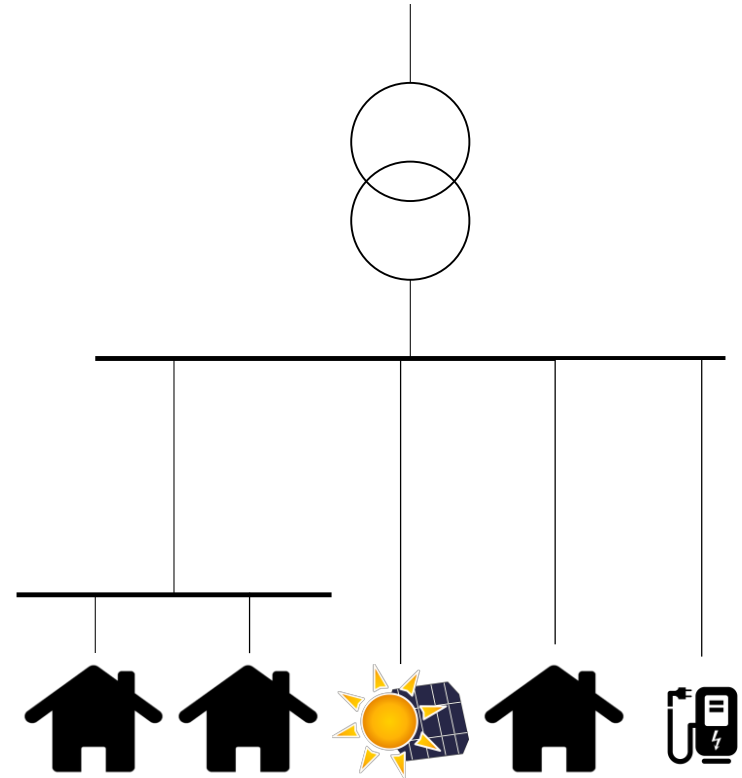
# 1. Motivation

- Distributed generation



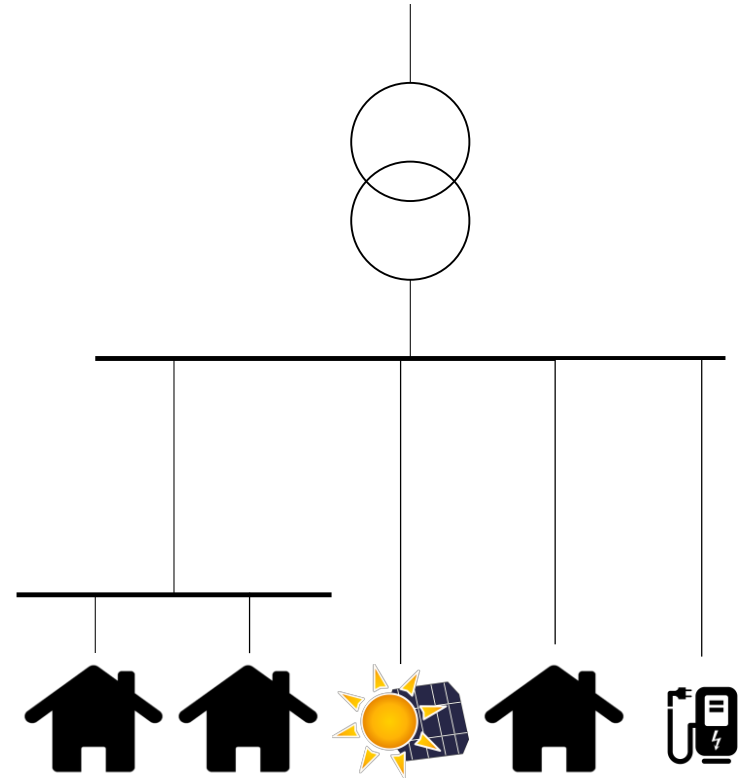
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- New types of load, e.g., charging station



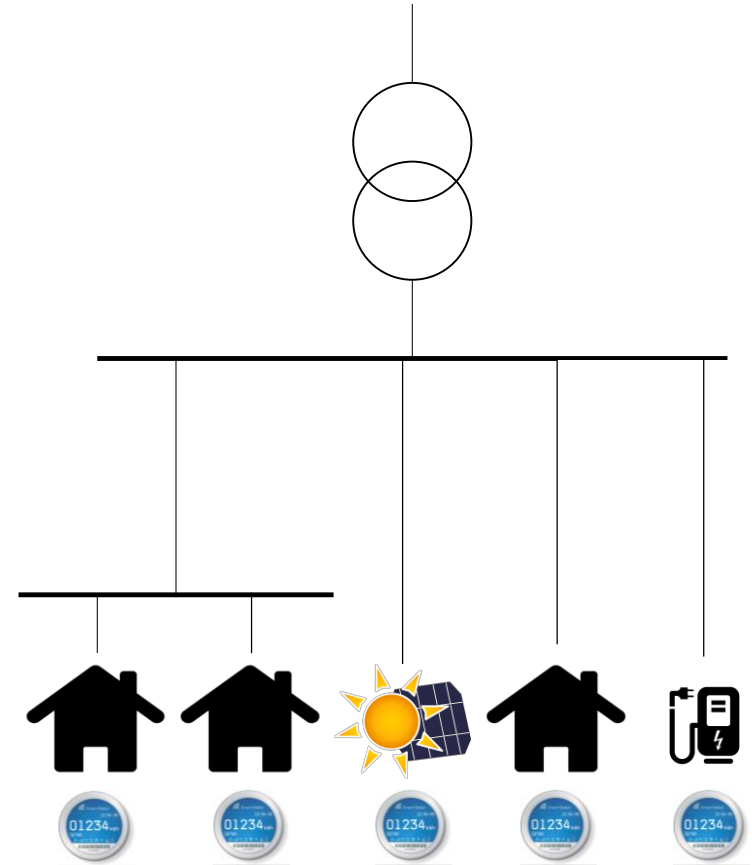
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- Distributed generation
- New types of load, e.g., charging station
- Increasing “smartness” at prosumers



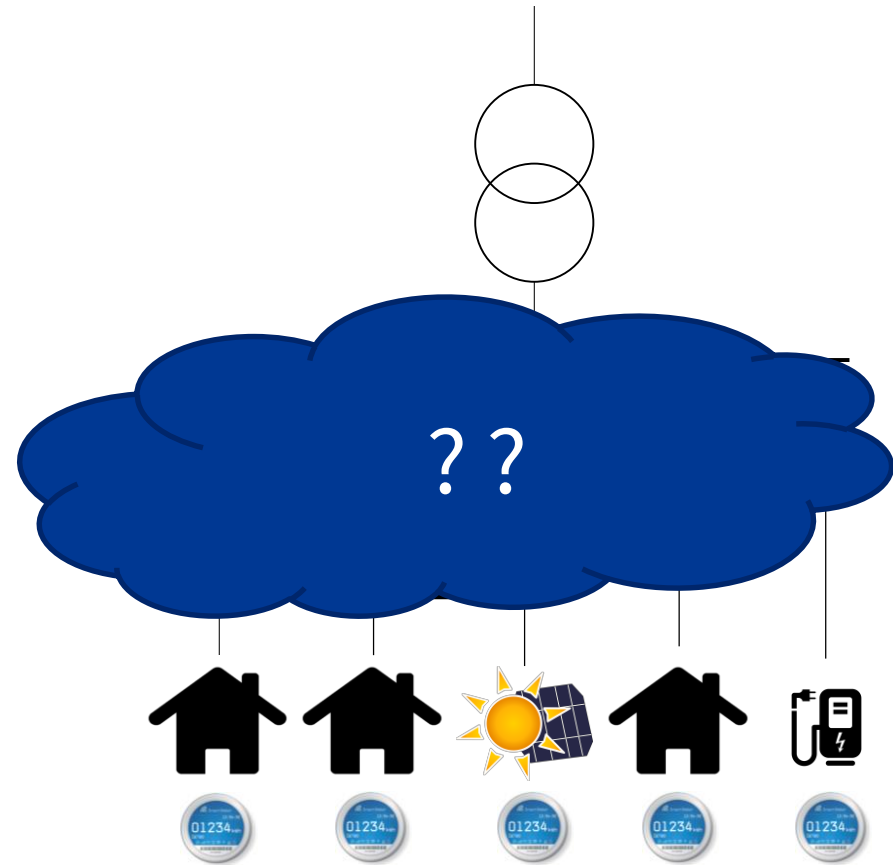
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- *Special case:* Low voltage grid
  - Data available via smart metering devices, but high communication effort



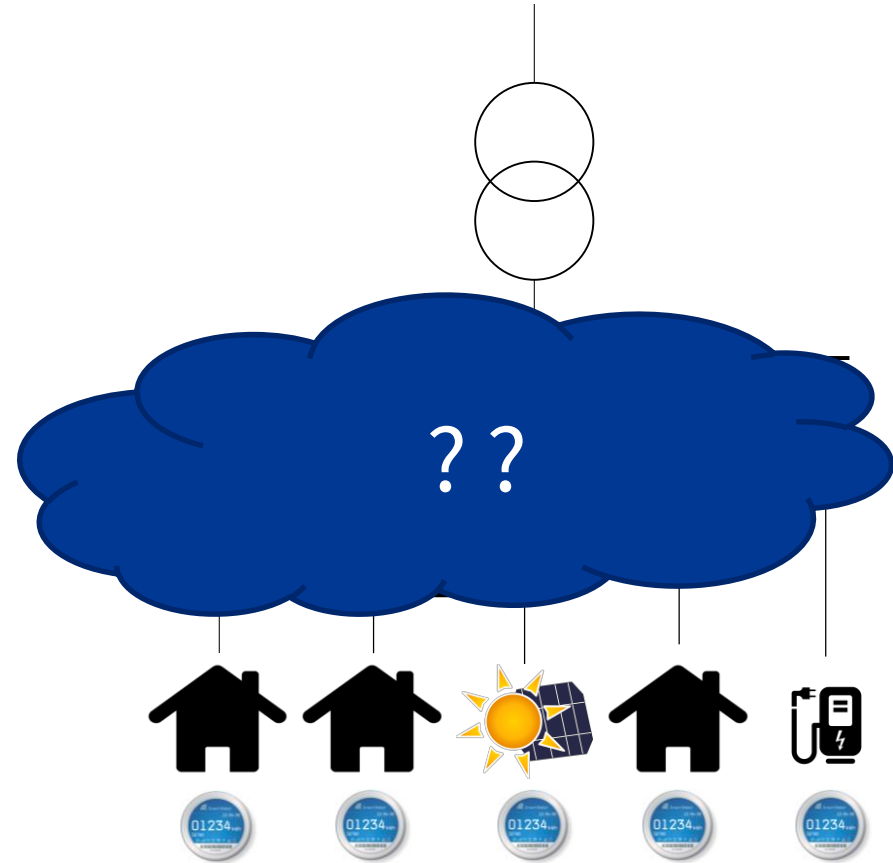
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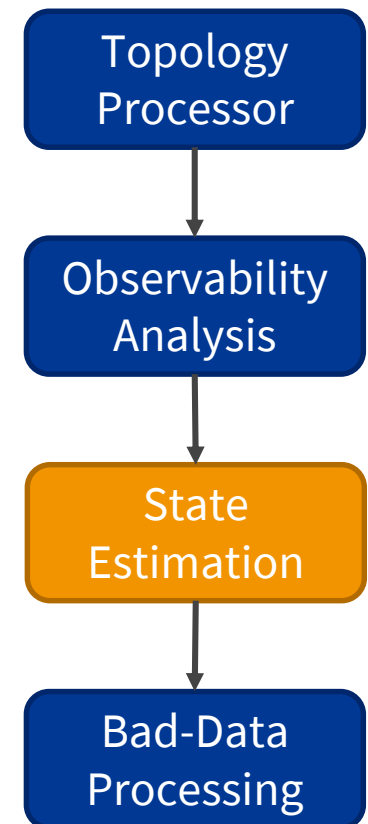
➔ Data-driven State Estimation (SE)





### Goal of State Estimation?

- Infer system state from a subset of measurements

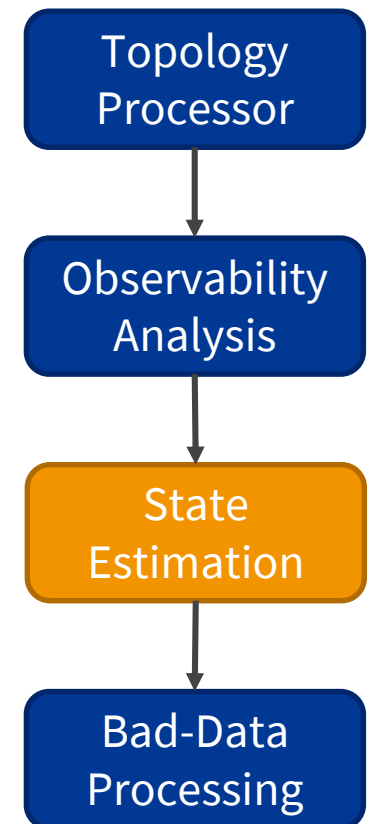


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### State Estimation

- Static State Estimation
- Multiarea State Estimation
- Forecasting State Estimation



## 2. State Estimation (1/2) [1, 2, 3]

### Goal of State Estimation?

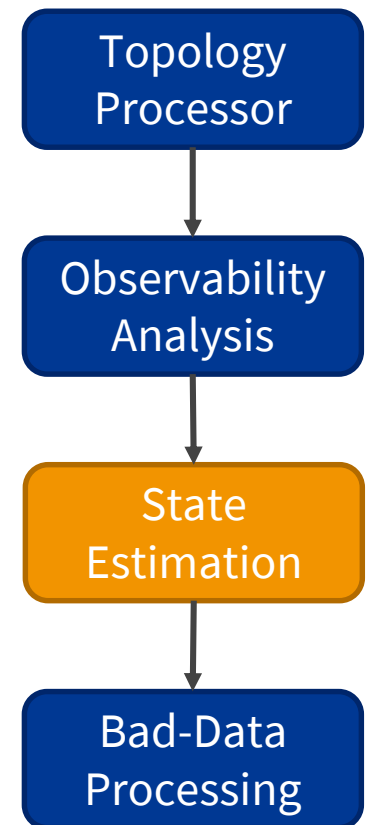
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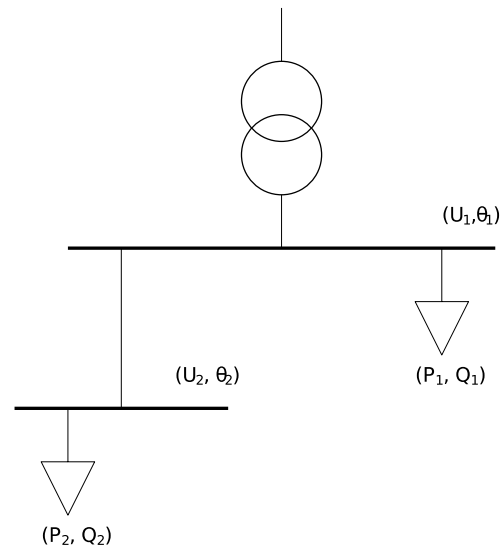
### Distribution System State Estimation

- Optimization Problem [4]
- Bayesian Network [5]
- Consensus Algorithms [6, 7]
- Machine Learning [8, 9]



### What is the state of a system?

- $x = [U_1, \dots, U_N, \theta_1, \dots, \theta_N] \in \mathbb{R}^{2N}$
- $z \in \mathbb{R}^L, L > 2N, (P, Q, U \text{ at busses})$



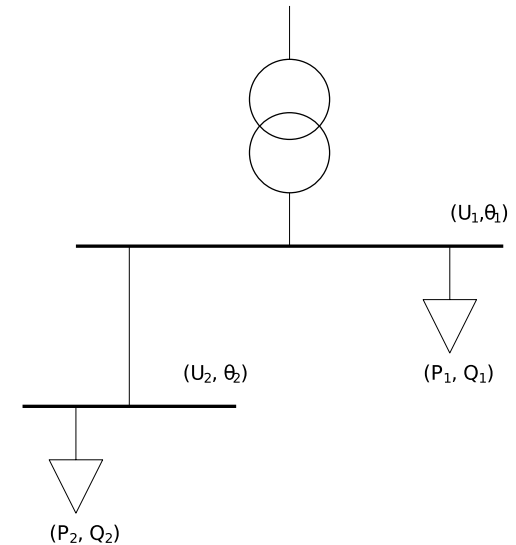
**Exemplary low voltage grid**

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### Relation

- $z = h(x) + n$
- $h(\cdot)$  is a set of nonlinear functions defined by Kirchhoff's laws and the power network admittance matrix,  $n$  estimation error



**Exemplary low voltage grid**

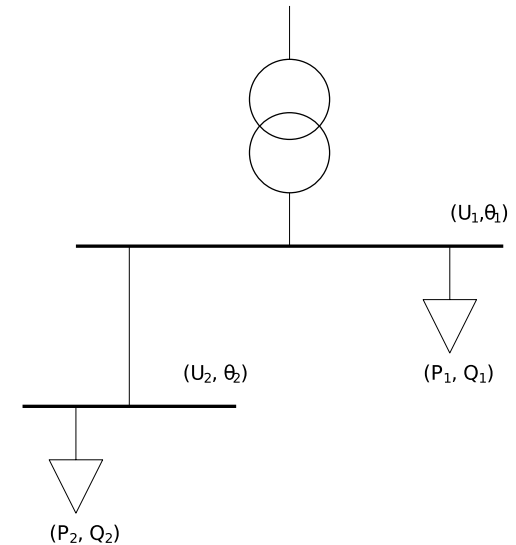
## 2. State Estimation (2/2) [1, 2, 3]

### What is the state of a system?

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Exemplary low voltage grid

### Traditional State Estimation Solver

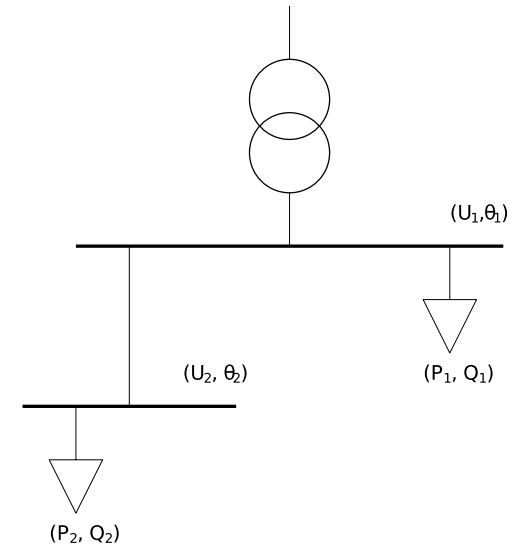
- $\hat{x} = \arg \min_x [z - h(x)]^T W^{-1} [z - h(x)]$
- Using Weighted Least Squares method

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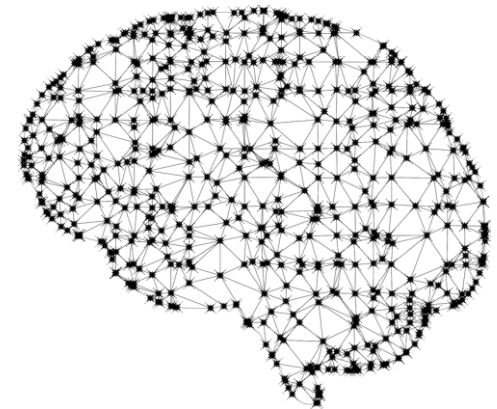
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### Traditional State Estimation Solver

- $\hat{x} = \arg \min_x [z - h(x)]^T W^{-1} [z - h(x)]$
- Using Weighted Least Squares method
- function  $h(x)$  requires grid topology information

### Data-Driven State Estimation

- $X = [U_1, \dots, U_N, \theta_1, \dots, \theta_N, P_1, \dots, P_M, Q_1, \dots, Q_N] \in \mathbb{R}^{2(N+M)}$
- $Y_t = X_t, t \leq 2(N + M)$
- $\bar{X}_t = X \setminus X_t$



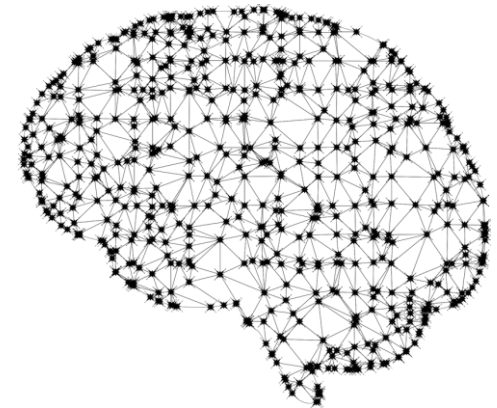


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### Machine Learning Model

- $\hat{Y}_t = f(\bar{X}_t)$
  - Model fitting on training data
  - Model evaluation on test/validation data
- Estimation of one single output parameter requires all input parameters



### 3.1. Dependency Graph Modelling

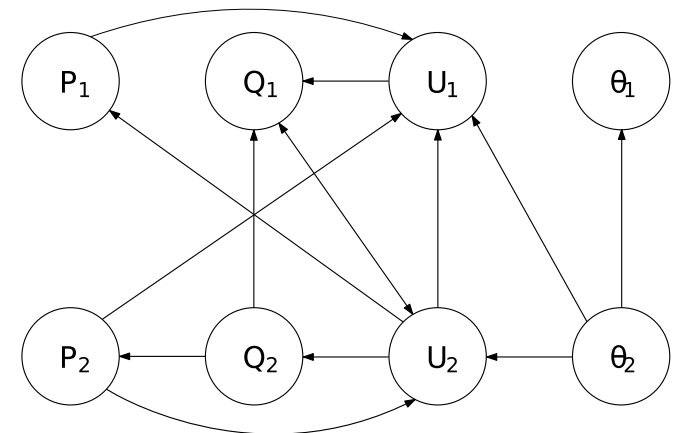
**Input:**  $X \in \mathbb{R}^{2(N+M)}$

**Output:** Adjacency matrix  $A$

#### Dependency Graph (DG)

- Correlation analysis
- (Absolute Difference analysis)
- (Logical Post processing, e.g., remove dependencies between two p values)
- Selection of  $n$  most influencing parameters

➔ directed graph as adjacency matrix

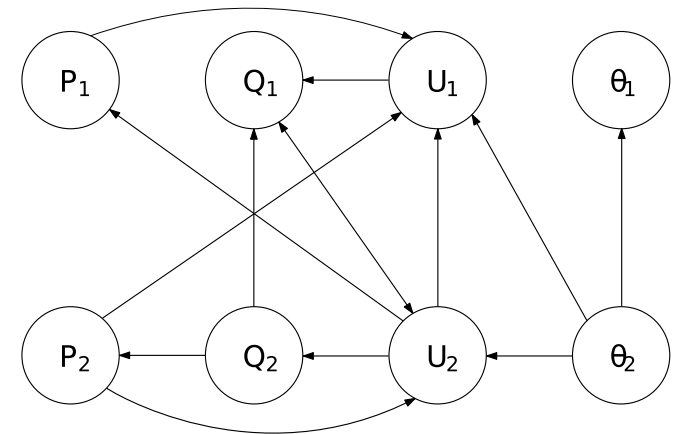


**Exemplary dependency graph**

### 3.2. Machine Learning

**Input:**  $X \in \mathbb{R}^{2(N+M)}, A$

**Output:**  $\hat{Y}$  for each single parameter



Exemplary dependency graph

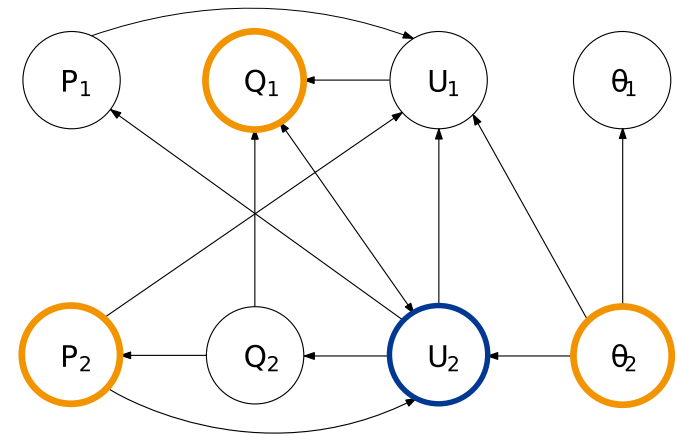
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#### Machine Learning

- One ML model for each node in the DG
- Input parameter taken from neighboring nodes



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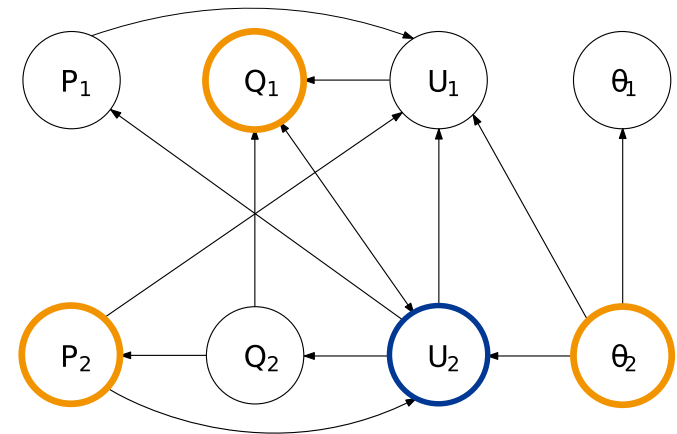
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Exemplary dependency graph

#### Prediction of multiple parameters

- Estimate parameter where all incoming nodes are available
- Iterate through the DG

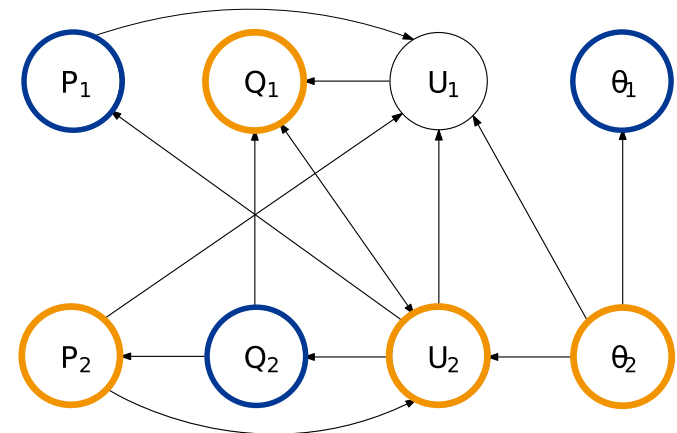
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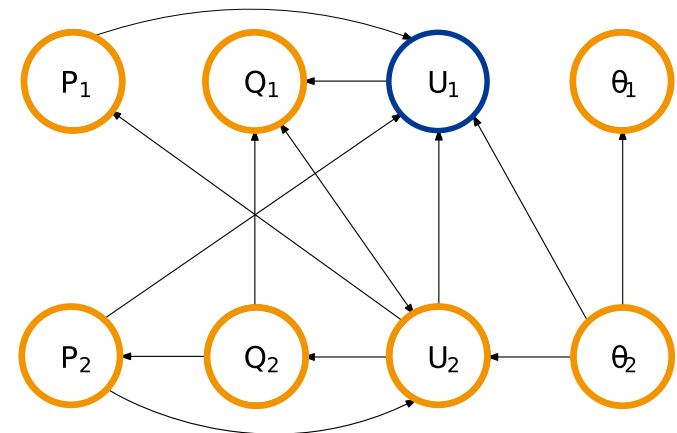
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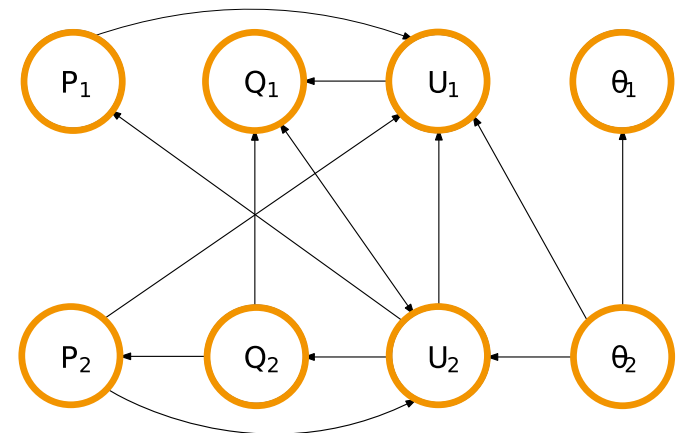
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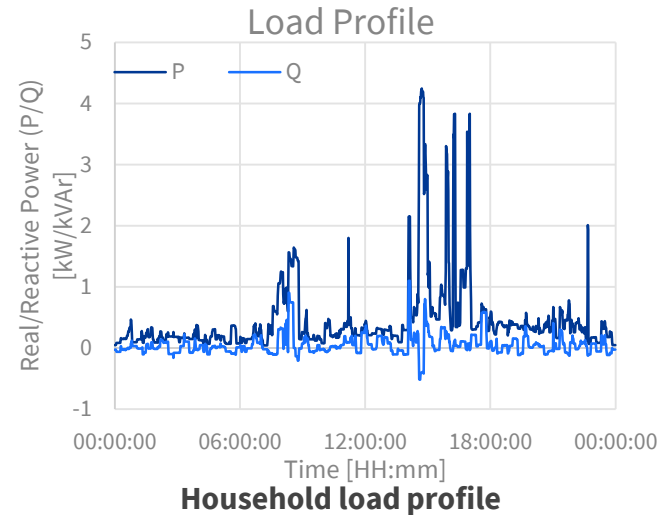
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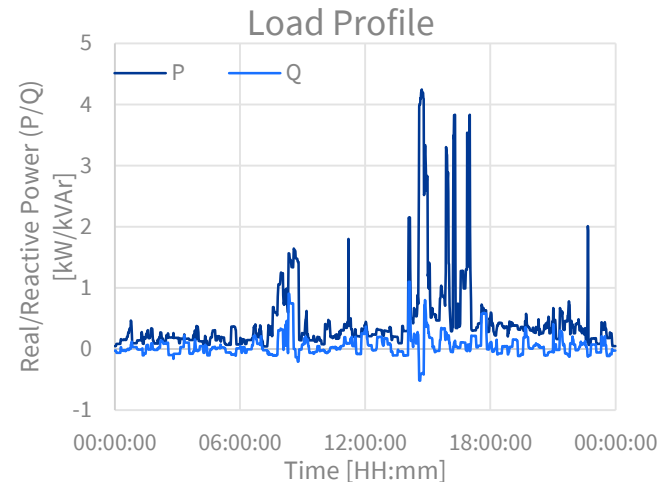
### Data Sampling Strategies

- Realistic load profiles and a power flow solver
  - Load profiles [10] + DIgSILENT PowerFactory

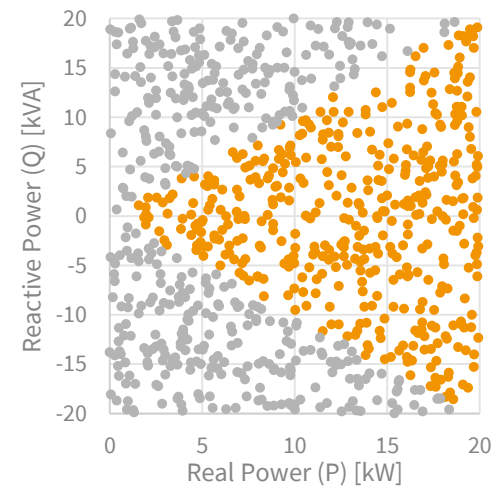


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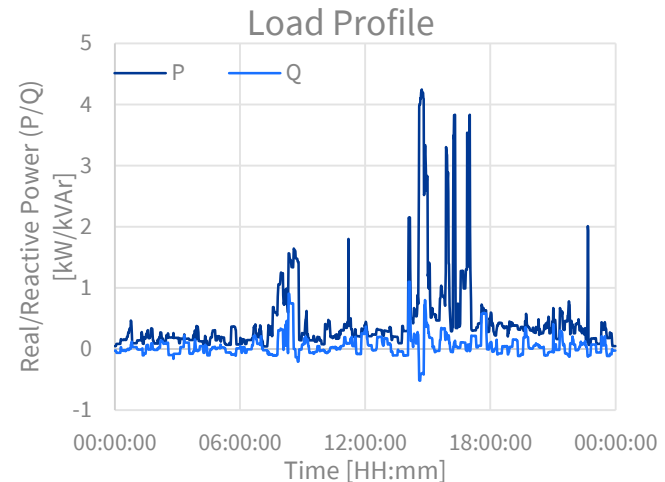
Household load profile



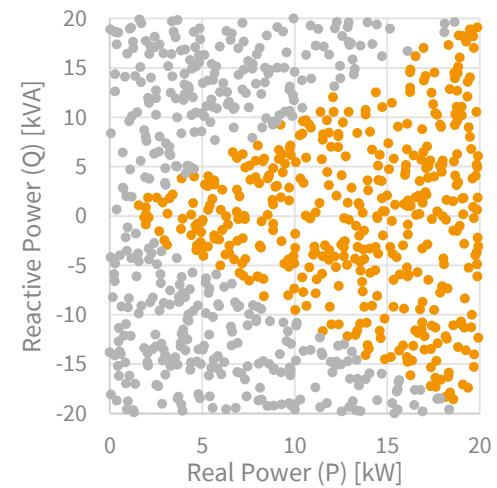
MC simulated load data

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- One-at-a-time sensitivity analysis of the power grid on P, Q of each load
  - Result of pulse measurements



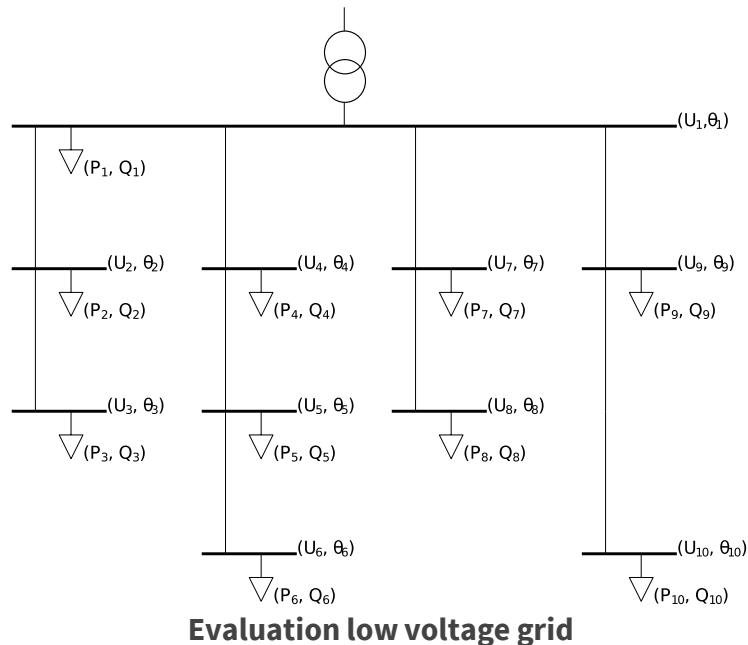
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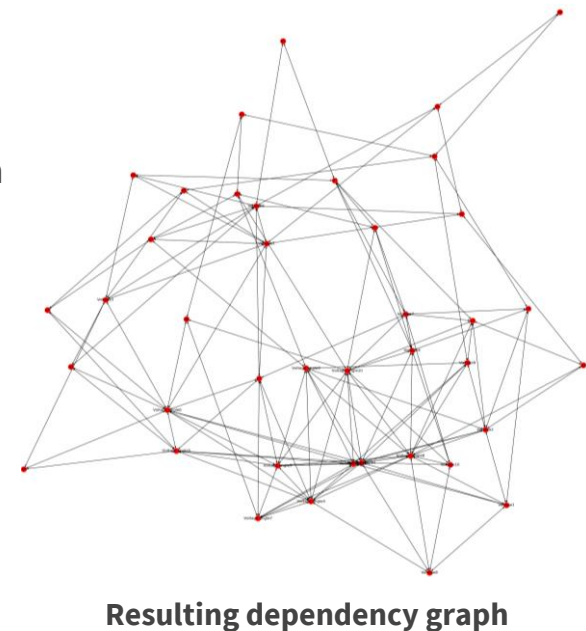
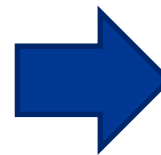
MC simulated load data

### Setup

- Low voltage grid with 10 household loads  $\rightarrow$  40 parameter
- Monte-Carlo samples ( $P \in [0 \text{ kW}, 20 \text{ kW}]$ ,  $Q \in [-20 \text{ kVAr}, 20 \text{ kVAr}]$ )
- Voltage magnitude and angle calculation by PowerFactory<sup>1</sup> using the sampled ( $P$ ,  $Q$ ) values



Dependency graph  
creation



## 4. Preliminary Results

### ML Evaluation

- Three different models
- 20 input parameter for each of the 40 models
- 5-fold-cross validation

$P$	[0 kW, 20 kW]
$Q$	[-20 kVAr, 20 kVAr]
$U$	[204 V, 232 V]
$\theta$	[-4.27°, 0.86°]

Parameter Ranges

Parameter	Linear Regression	KNN	Random Forest
$U_1$	<b>0.021 V</b>	0.13 V	0.358 V
$\theta_2$	<b>0.001 °</b>	0.019 °	0.123 °
...	...	...	...
$P_1$	<b>0.057 kW</b>	2.725 kW	4.5 kW
$Q_7$	<b>0.075 kVA</b>	0.823 kVA	2.421 kVA
...	...	...	...

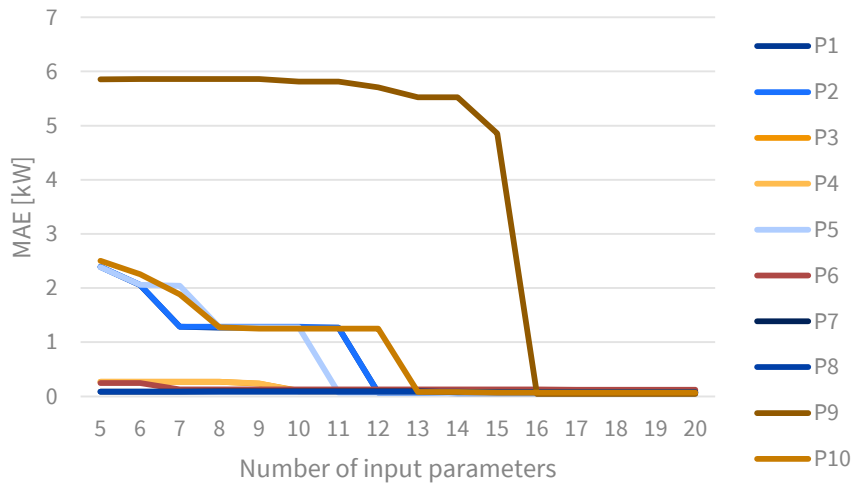
Excerpt of Mean Absolute Error using 20 input parameter in the dependency graph



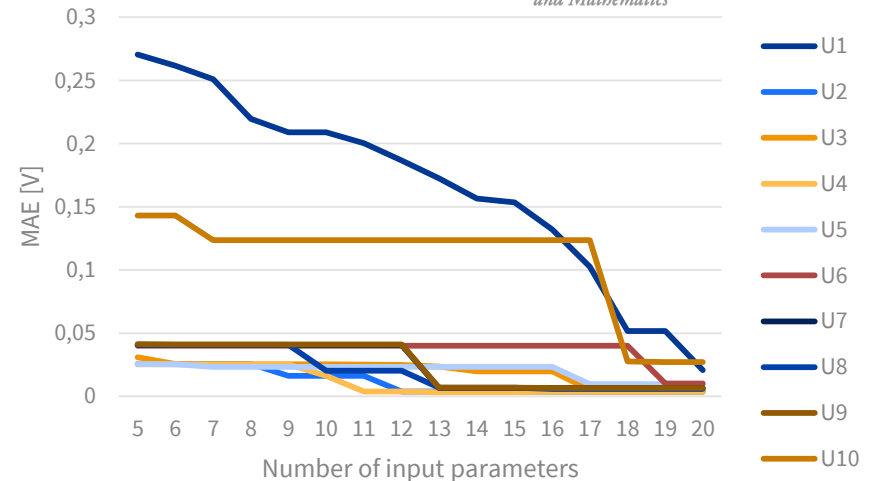
## 4. Preliminary Results

### Sensitivity of the DG creation

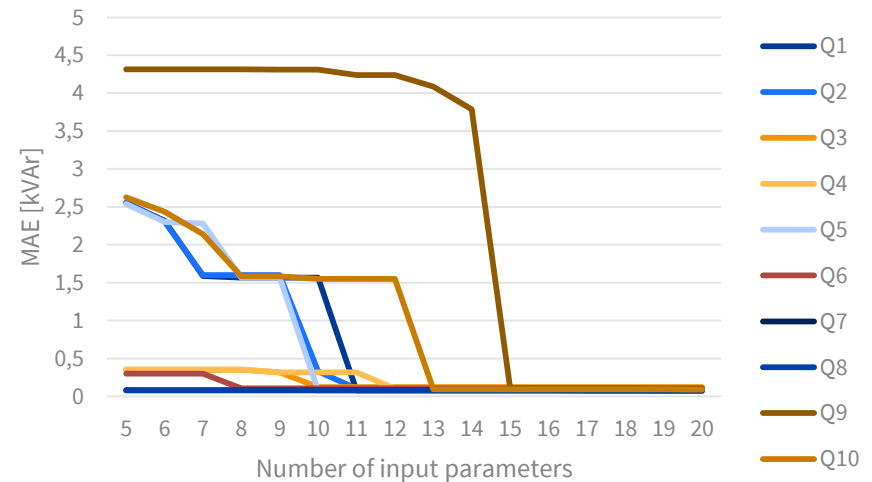
- 13+ from 40 parameter yield reasonable results
- Predictability depends on parameter selection strategy and grid location



Mean Absolute Error estimating real power



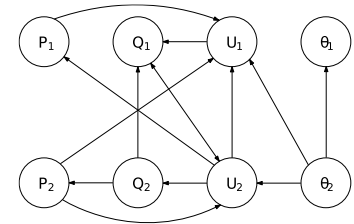
Mean Absolute Error estimating voltage



Mean Absolute Error estimating reactive power

## 5. Conclusion

- Conclusion
  - Data-driven static state estimation seems promising when using a dependency graph to reduce the input parameter set
  - Applicable to distribution systems where the topology is not known
- Open Points
  - Include plausibility checks and data pre/post processing
  - Increase accuracy by rechecking all available single parameter models
  - Comparison to calculated state estimation with inaccurate topology information
  - Performance evaluation



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- [7] F. S. Cattivelli and A. H. Sayed, “Diffusion strategies for distributed Kalman filtering and smoothing”. *IEEE Transaction on Automatic Control*, Sep 2010.
- [8] J. Yu, Y. Weng and R. Rajagopal, "Robust mapping rule estimation for power flow analysis in distribution grids". *North American Power Symposium (NAPS)*, Sep 2017.
- [9] J. Cardona, T. Gill, and S. Powell, “CS229 : Machine Learning Models for Inverse Power Flow in the Grid”. *CS229 Final Report*, 2017.
- [10] Tjarko Tjaden, Bergner Joseph, and Volker Quaschnig. “Repräsentative elektrische Lastprofile für Wohngebäude in Deutschland auf 1-sekündiger Datenbasis”. *HTW Berlin*, Nov 2015.



***Thank you for your attention!***

***Time for Discussions!***

